# Automatization of Pin Fin Heat Sink Design with Geometric and Fluid Constraints

Giovanni Filomeno<sup>12</sup>, Bastian Krüger<sup>12</sup>, Peter Tenberge<sup>1</sup>, Dirk Dennin<sup>2</sup>

<sup>1</sup>Industrial and Automotive Drivetrains, Ruhr-University of Bochum, Germany

<sup>2</sup> Advanced Development Transmission and Powertrain Simulation, BMW-Group, Munich, Germany Email: giovanni.filomeno@ruhr-uni-bochum.de, giovanni.filomeno@bmw.de, bastian.kb.krueger@bmw.de, peter.tenberge@ruhr-uni-bochum.de, dirk.dennin@bmw.de

Abstract— The sizing of the cooling system is one of the most crucial parts of the design of power electronics since it has a high impact on the overall performance of the packages as well as the lifetime of the chips. The high temperature causes irreversible damage and increases the cost for maintenances and substitutions. However, during the design of the package, some geometric constraints can occur, such as maximum height or width. Moreover, limitations about volume rate and fluid temperature must be taken into account. This work aims to create a tool that can automatize the design of the heat sink cooling system with geometric constraints. The analytical model can consider in-line and staggered configurations. In this study, a genetic algorithm is applied as the optimization algorithm in order to find a solution which respects the boundary and fluid constraints and minimize the heat sink volume. Numerical simulations for the resulted geometries have been performed to validate the tool. The results of the numerical simulations show an error between the numerical and the expected maximum temperature of the plate lower than 2% and 3% for in-line and staggered configuration, respectively. The model can be applied over a wide range of application, and it can be easily adapted to different material and different cooling liquid.

Index Terms-heat sink design, numerical simulations, power electronics, optimisation

## NOMENCLATURE

- D Pin diameter [m]
- W Width of heat sink [m]
- L Length of heat sink [m]
- Η Pin height [m]
- t Thickness [m]
- $S_L$ Pin space in the stream-wise direction [m]
- $S_{T}$ Pin space in the span-wise direction [m]
- $S_D$ Diagonal space [m]  $\equiv \sqrt{S_L^2 + 0.25 \cdot S_T^2}$
- $S_L^*$ Normalised stream-wise pitch  $\equiv S_L/D$
- $S_T^*$ Normalised span-wise pitch  $\equiv S_T/D$
- $S_D^*$ Normalised diagonal pitch  $\equiv S_D/D$
- $N_L$ Number of fins in the stream-wise direction
- $N_T$ Number of fins in the span-wise direction
- Ν Total number of fins
- Specific heat  $[J \cdot kg^{-1} \cdot K^{-1}]$  $C_p$
- $k_{f}$ Thermal conductivity of the fluid  $[W \cdot m^{-1} \cdot K^{-1}]$

- $\dot{V}$ Volume flow rate  $[L \cdot s^{-1}]$
- Mass flow rate  $[kg \cdot s^{-1}] \equiv \dot{V} \cdot \rho \cdot 0.001/60$ т
- μ Absolute viscosity of fluid [Pa·s]
- Kinematic viscosity of fluid [m<sup>2</sup>·s<sup>-1</sup>]  $\boldsymbol{n}$
- ρ Density of fluid [kg·m<sup>-3</sup>]
- Pr
- Prandtl number  $\equiv c_p \cdot \mu / k_f$
- Q Dissipated power [W]
- Reynolds number evaluated with the maximum Re<sub>D</sub> velocity between fins  $\equiv D \cdot U_{max}/\nu$
- U Velocity of fluid  $[m \cdot s^{-1}]$
- Т Absolute temperature [K]

# ASSUMPTIONS

- 1. Adiabatic lateral wall of the base plate
- 2. Adiabatic bottom face of fins
- 3. Isotropic material
- 4. Uniform velocity
- 5. Height of the cooling channel = height of the fins
- 6. Fully developed heat and fluid flow
- 7. Constant density of the material
- 8. Constant heat transfer of the material
- 9. Steady and laminar flow

## I. INTRODUCTION

During the last two decades, the reducing size challenge in electronic products has become increasingly popular due to the increase of interest towards the hybrid powertrain development. The increase in the use of power electronics has also increased the attention to reducing costs and space. For this purpose, the design of an efficient cooling system plays a vital role since the maximum allowable temperature of the junctions determines the lifetime of the package. Nowadays, the most used cooling system is the aluminium Pin-Fin heat sink. It provides a good compromise between efficiency and cost due to the vast plate region that reduces the thermal resistance of the package. Two key classification criteria used for heat sinks are the topology and density of the fins, with the topology usually classified as in-line or staggered. (see Fig. 1-a and Fig. 1-b).

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Figure 1-a. Nomenclature for In-Line configuration



Figure 1-b. Nomenclature for Staggered configuration

Over the years there have been many studies performed into the optimal geometric parameter combinations of Pin-Fin heat sinks. A particular study about the effect of the separation between two fins shows that the optimum separation in span-wise direction is  $1.0\pm0.2 \text{ mm} < S_T < 3.0\pm0.2 \text{ mm}$  for both in-line or staggered configuration as well as  $7.6\pm0.2 \text{ mm}$  and  $7.8\pm0.2 \text{ mm}$  in stream-wise direction for in-line and staggered, respectively [1].

The same authors also studied the correlation between the fins' distance and the total dimension. The study shows that the best solution can be achieved inside the range between  $0.004 \le S_T/W \le 0.332$  and  $0.033 \le S_L/L \le 0.152$ [2]. The technical investigation about the shape of the fins was resolved in 1996 in Sweden. In the KTH laboratories, the best shape for the Pin-Fin turned out to be elliptical or circular for high and mid-range velocity, respectively [3]. The fin space ratio had also been studied in 1998. During this experimental study, the researcher found 2.5D both in line and staggered. They also studied the effects of missing fins [4]. In 1996, a study conducted with experimental data discovered that the optimal ratio between the length and the diameter of the cylinder Pin-Fin falls within the range of  $6.2 \le H/D \le 20$  [5]. In 2004, a Canadian paper presented the results of an optimisation algorithm that took into account the entropy of the system with respect to the ratio between the plate and fins dimensions [6].

The effect of Pin-Fin density was investigated in 2010. The presented results show that the thermal resistance is influenced by the flow pattern and that the optimal fin spacing ratio  $S_T/D$  is 0.5 and 0.3 for 5 mm and 11 mm fin

length respectively [7]. Regarding the thermal characteristics, in 1986, studies found a relation between the fin position and the thermal resistance. During the experiments, the bottom tubes immersed in a hot fluid flow presented a different average heat transfer coefficient concerning the higher tubes [8]. One year later, a similar study in Switzerland found the relation between heat transfer and space as well as between pressure drop and space [9]. On the same topic, an experimental study was conducted with two arrays of tubes and the Reynolds number in a range starting from 7500 to 32000. The result shows that the pressure drop and the heat transfer are strongly influenced by the pitch distance [10]. Same results were achieved in Japan, where the variation of heat transfer and pressure drop are compared with the change of the Nusselt number, which represents the ratio between convective and conductive heat transfer [11]. According to the literature, it is thus clear that all the studies optimised a specific geometric parameter concerning either the entropy or the fluid characteristics. In the literature, there are no constraints to space or fluid characteristics. In this study, all the geometric parameter are isolated and constrained to deal with engineering applications.

## II. MODEL DEVELOPMENT

The thermal resistance of the heat sink is defined as:

$$R_{hs} = \frac{\Delta T}{Q} \tag{1}$$

where  $\Delta T = T_{IGBT} - T_f$  is the difference between the maximum IGBT temperature and  $T_f$  which is the temperature of incoming fluid. The dissipated power Q can be divided into three groups:

$$Q = Q_c + Q_{sw} + Q_b \approx Q_c + Q_{sw} \tag{2}$$

where  $Q_c$  and  $Q_{sw}$  are the conduction and switching losses, respectively. The blocking losses  $Q_b$  are normally neglected. Further details are presented in the literature [12, 13].

The total resistance of the heat sink can be written as the sum of three different resistances as:

$$R_{hs} = R_m + R_e + R_t \tag{3}$$

where  $R_e$  is the additional resistance between the IGBT and the heat sink is,  $R_m$  is the resistance of the base and  $R_t$ is the resistance of the fins and the plate (see Fig. 2).



Figure 2. Thermal conductivity model

 $R_m$  can be defined as:

$$R_m = \frac{t}{k \cdot L \cdot W} \tag{4}$$

where k is the thermal conductivity of heat sink material.  $R_t$  can be written as follows:

$$R_{t} = \frac{1}{\frac{N}{R_{fin}} + \frac{1}{R_{b}}} = \frac{1}{\frac{N}{h_{fin} \cdot A_{fin} \cdot \eta_{fin}} + \frac{1}{h_{b} \cdot A_{b}}}$$
(5)

where  $R_{fin}$  and  $R_b$  are the thermal resistances of the fins and the plate, respectively, which are in contact with the fluid,  $A_{fin}$  and  $A_b$  are the contact area fluid-solid of the fin and plate, respectively. The mean heat transfer coefficients  $h_{fin}$  and  $h_b$  can be written as [14]:

$$h_{b} = \frac{0.75 \cdot k_{f}}{D} \cdot \sqrt[2]{\frac{S_{T}^{*} - 1}{N_{L} \cdot S_{L}^{*} \cdot S_{T}^{*}}} \cdot \sqrt[2]{\operatorname{Re}_{D}} \cdot \sqrt[3]{\operatorname{Pr}}$$

$$h_{fin} = \frac{C_{1} \cdot k_{f}}{D} \cdot \sqrt[2]{\operatorname{Re}_{D}} \cdot \sqrt[3]{\operatorname{Pr}}$$
(6)

 $C_1$  is a dimensionless constant which depends on the arrangement of the pins, as it can be seen in Equation (7) [14].

$$C_{1} = \begin{cases} 0.2 + \exp(-0.55 \cdot S_{L}^{*}) \cdot S_{T}^{*0.285} \cdot S_{L}^{*0.212}, in-line \\ \frac{0.61 \cdot S_{T}^{*0.091} \cdot S_{L}^{*0.052}}{1 - \exp(-1.09 \cdot S_{L}^{*})}, staggered \end{cases}$$
(7)

The contact area can be calculated as:

$$A_{fin} = \pi \cdot D \cdot H$$

$$A_{b} = L \cdot W - N \cdot \frac{\pi \cdot D^{2}}{4}$$
(8)

The fin resistance includes  $\eta_{fin}$ , which represents the efficiency of the fin and which can be calculated as:

$$\eta_{fin} = \frac{\tanh(m \cdot H)}{m \cdot H}$$

$$m = \sqrt[2]{\frac{4 \cdot h_{fin}}{k \cdot D}}$$
(9)

By combining all the equations and isolating the length of the fins H, we obtain the following system:

$$\tau^* \cdot H^{\frac{1}{4}} \cdot \tanh\left(\varepsilon^* \cdot H^{\frac{3}{4}}\right) + z^* - H^{\frac{1}{2}} = 0$$
  
$$\tau^* = \tau \cdot N \cdot \pi \cdot \frac{C_1^{\frac{3}{2}}}{D} \cdot \sqrt[2]{\Pr} \cdot 2 \cdot \sqrt[2]{\frac{1}{k}} \cdot k_f^{\frac{3}{2}} \cdot \alpha^{\frac{3}{4}}$$
  
$$z^* = \tau \cdot \frac{0.75}{D} \cdot k_f \cdot \sqrt[2]{\frac{S_T^* - 1}{N_L \cdot S_L^* \cdot S_T^*}} \cdot \sqrt[3]{\Pr} \cdot \sqrt[2]{\alpha}$$
(10)  
$$\cdot \left(L \cdot W - \frac{N \cdot \pi \cdot D^2}{4}\right)$$
  
$$\alpha = \frac{D \cdot c \cdot V \cdot 0.001}{L \cdot 60}$$

$$\tau = \left(\frac{\Delta T}{Q} - R_m - R_e\right)$$
$$\varepsilon^* = \sqrt[2]{\frac{4 \cdot C_1 \cdot k_f \cdot \Pr^{\frac{1}{3}} \cdot \alpha^{\frac{1}{2}}}{k \cdot D^2}}$$
$$c = \max\left\{\frac{S_T^*}{S_T^* - 1}, \frac{S_T^*}{S_D^* - 1}\right\}$$

The system presented in Equation (10) contains the geometry parameters and the pump characteristics. These characteristics can be constrained as follows:

$$L_{IGBT} \leq L \leq L_{MAX}$$

$$W_{IGBT} \leq W \leq W_{MAX}$$

$$0.004 \cdot W \leq S_T \leq 0.332 \cdot W$$

$$0.033 \cdot L \leq S_L \leq 0.152 \cdot L$$

$$\vdots \\ V_{\min} \leq V \leq V_{\max}$$

$$T_{\min} \leq T_f \leq T_{\max}$$

$$H \leq H_{\max}$$

$$t_{IGBT} \leq t \leq 2 \cdot t_{IGBT}$$

$$(11)$$

In the literature, several methods could be used to solve non-linear problems. Most of these methods however, have additional requirements such as convexity or continuity, or they can be applied only to a specific type of problem such as Quadratic Programming.

By considering these limitations, further methods have been implemented, such as Genetic Algorithm, Ant Colony Optimization and Particle Swarm Optimization [15, 16, 17]. The problem is given by nonlinear objective function f, which is to be minimised with respect to the design variable  $\bar{x}$ ={L, W, S<sub>T</sub>, S<sub>L</sub>,  $\dot{V}$ , T, D, t} and to the inequality and non-linear equality constraints presented in Equation (11).

The function to minimise is the volume of the IGBT; however since the H is linearly dependent on the design variable  $\bar{x}$ , it was included into the fitness function as a penalty value, as presented in Equation (12).

$$f_{fitness} = L \cdot W \cdot t + N \cdot \frac{\pi \cdot D^2}{4} \cdot H$$
  
+(bool)(H > H<sub>max</sub>) \cdot 10<sup>6</sup> (12)

To solve this problem, a genetic algorithm has been used with 800 generations and 350 as population size. Moreover, the crossover fraction and the constraint tolerance were 0.8 and 0.001, respectively.

## III. REFRIGERANT

T [K]	µ [Pa∙s]	$\nu [m^2 \cdot s^{-1}]$	ρ [kg·m <sup>-3</sup> ]	$c_p [J \cdot kg^{-1} \cdot K^{-1}]$	$k_f [W \cdot m^{-1} \cdot K^{-1}]$
278.15	0.00748	6.91400E-06	1081.6		0.382650918
283.15	0.00610	5.64800E-06	1079.0	3250.00	0.385676006
288.15	0.00505	4.69200E-06	1076.3		0.388693026
293.15	0.00424	3.94600E-06	1073.5	3310.00	0.391742873
298.15	0.00360	3.35900E-06	1070.7		0.394868824
303.15	0.00309	2.89000E-06	1067.8	3370.00	0.398095512
308.15	0.00268	2.51300E-06	1064.8		0.401402361
313.15	0.00234	2.20400E-06	1061.8	3420.00	0.404617044
318.15	0.00206	1.94800E-06	1058.6		0.407607237
323.15	0.00184	1.73900E-06	1055.4	3470.00	0.410498206
328.15	0.00164	1.55800E-06	1052.1		0.413453304
333.15	0.00147	1.40600E-06	1048.8	3520.00	0.416569059
338.15	0.00134	1.27800E-06	1045.4		0.419858628
343.15	0.00121	1.16400E-06	1041.9	3560.00	0.423091604
348.15	0.00111	1.06800E-06	1038.3		0.426080508
353.15	0.00102	9.84000E-07	1034.7	3590.00	0.428971478
358.15	0.00094	9.09000E-07	1031.0		0.431944832
363.15	0.00087	8.43000E-07	1027.2	3620.00	0.435041165

 $k_f = a \cdot T + b$ 

 $\rho = c \cdot T^2 + d \cdot T + e$ 

 $c_p = f \cdot T^6 + g \cdot T^5 + h \cdot T^4 + i \cdot T^3 + l \cdot T^2 + m \cdot T + n$ 

 $\mu = o \cdot T + p$ 

 $v = q \cdot T + r$ 

TABLE I. FLUID PROPERTIES

The fluid considered for this application is a mix 1:1 of ethylene glycol and water. Table I presents the data used for the calculations. Additionally, all the fluid properties are interpolated over the temperature in order to obtain a continuous domain for the fluid characteristics. Equation (13) shows the considered interpolations:

a = 6.16786E - 04b = 2.11186E - 01c = -1.449690E - 03d = 2.896245E - 01e = 1.113209E + 03f = 3.439972E - 11g = 6.348257E - 08h = -4.875081E - 05i = 1.994455E - 02l = -4.608157E + 00m = 5.811936E + 02n = -2.907926E + 04o = -6.5766563467E - 05p = 2.3757437465E - 02q = -6E - 08r = 2E - 05

# IV. RESULTS

The purpose of this section is to validate the analytical findings with the use of CFD Software STAR-CCM+. The examples are computed assuming aluminium as the material of the heat-sink with a value of  $237 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  for the thermal conductivity. For the optimisation, using the inequalities presented in Equation (11), the following constraints are applied:

 $\begin{array}{l} 32mm \leq L \leq 60mm \\ 18mm \leq W \leq 45mm \\ 0.004 \cdot W \leq S_T \leq 0.332 \cdot W \\ 0.033 \cdot L \leq S_L \leq 0.152 \cdot L \\ \cdot \\ 1L/\min \leq V \leq 8L/\min \\ 30^\circ C \leq T_f \leq 80^\circ C \\ 3mm \leq t \leq 6mm \end{array} \tag{14}$ 

655

(13)

Table II shows the obtained values for the geometry. In order to validate the results, the derived geometry has been replicated into the CFD software. By applying the same boundary conditions, the error between the maximum temperature of the plate recorded by the program and that entered as input by the genetic algorithm is calculated.

TABLE II: CONSTRAINED OPTIMISATION CASES

Parameters	Case A	Case B	
L [MM]	50	37	
W [MM]	40	26	
T [MM]	5	5	
$N_L$	10	18	
N <sub>T</sub>	8	13	
Type	IN-LINE	STAGGERED	
D [MM]	2	1	
$S_L$ [MM]	5	2	
$S_{T}[MM]$	5	2	
Н [ММ]	4.3	4.2	
$T_f$ [°C]	55	55	
POWER [W]	1154	2000	
$T_{MAX}$ [°C]	140	175	
$T_{CFD}$ [°C]	142.63	178.82	
Error	1.88%	2.18%	

Fig. 3 and Fig. 4 present the results obtained with STAR-CCM+ of Case A and Case B, respectively.

The sub-figure .a and .b show the 3D overview and the temperature graph, respectively.

The two sub-figures .b prove that the simulation reaches the steady-state situation where the temperature remains constant.



Figure 3-a. IGBT Temperature graph of Case A



Figure 3-b. 3D View of Case A



Figure 4-a. IGBT Temperature graph of Case B



Figure 4-b. 3D View of Case B

## V. CONCLUSION

An analytic approach is presented in order to find the optimal heat sink design with geometric and pump constraints. The effects of velocity, pin density, temperature and thermal conductivity are examined with respect to their influence on the design. The designs respect the technical constraints, and the plate temperature exceeds the maximum allowable temperature with an error less of 2% and 3% for in-line and staggered configuration. The difference in temperature between the two setups was found in all the test cases analysed. The higher pressure drop, as well as the change in velocity direction, can be the causes of this deviation.

## CONFLICT OF INTEREST

The authors declare no conflict of interest.

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**Giovanni Filomeno** was born in Castellana Grotte, Italy, in 1993. He received the M.Sc. in Computational Mechanics from Technical University of Munich (TUM), the B.Sc. in Mechanical Engineering from Polytechnic University of Turin. He took part in a double degree project in Mechanical and Industrial Production Engineering at the Tongji University of Shanghai in academic year 2013-2014. He

works at the BMW-Group as Ph.D. candidate in collaboration with the Institute of Industrial and Automotive Drivetrains at Ruhr-University Bochum, Germany. His research interests are numerical methods, optimisation algorithms, mechanical design, hybrid transmissions, power electronics and statistical analysis.



**Bastian Krueger** was born in Ettenheim, Germany, in 1991. He received the B.Sc. and M.Sc. degree (with distinction) in mechanical engineering from the Karlsruhe Institute of Technology, Germany. He is currently pursuing his Ph.D. in mechanical engineering at BMW AG, Munich, Germany in cooperation with the Institute of Industrial and Automotive Drivetrains, Ruhr-University Bochum, Germany. His research interests include the

design, modelling and control of novel automotive powertrain systems.



**Prof. Dr.-Ing. Peter Tenberge**, born in 1956, studied Mechanical Engineering, majoring in Engineering Design at Ruhr University Bochum (RUB), Germany. Subsequently, he worked as a scientific assistant at the Chair of Machine Elements and Gears at RUB and finished his PhD on the topic of transmissions. From 1986 to 1994, he worked for Zahnradfabrik Friedrichshafen and Schaeffler, Germany, at the end as the manager for automotive components. From 1994 to 2012,

he was Professor for Machine Elements at the Technical University in Chemnitz, Germany. Since 2012, he was Professor for Industrial and Automotive Drivetrains at RUB in Bochum.



**Dr.-Ing. Dirk Dennin**, born in 1964, studied Mechanical Engineering, majoring in General Mechanical Engineering at Technical University of Munich (TUM), Germany. Subsequently, he worked as a scientific assistant at the Chair of Mechanics B at TUM and finished his PhD on the topic of vibration technology in gearboxes. Since 1996, he worked in several positions for BMW in Munich. Since 2009 he led the simulation at the predevelopment of transmission and drivetrain at

BMW in Munich.